## Supporting Information

## Chromatin unfolding by epigenetic modifications explained by dramatic impairment of internucleosome interactions: a multiscale computational study

## Chromatin coarse-grained model

Our work includes Monte Carlo simulations of 24-nucleosome arrays carried out with a
our coarse-grained chromatin model ${ }^{1-12}$. The model has been described in detail in ${ }^{3,7,10}$, and below we summarize the strategies used to treat each oligonucleosome component:

Nucleosome cores. The nucleosome protein core, excluding histone tails, with wrapped DNA is modelled as a rigid irregular body with 300 Debye-Hückel charges uniformly distributed on the nucleosome molecular surface. The charges are optimized to reproduce the full atom electric field around the nucleosome core by the Discrete Surface Charge Optimization (DiSCO) algorithm ${ }^{2}$, which solves the complete nonlinear Poisson-Boltzmann equation.

Flexible histone tails. Our original model considers the ten histone tails protruding out of each core (the N-termini of each $\mathrm{H} 2 \mathrm{~A}, \mathrm{H} 2 \mathrm{~B}, \mathrm{H} 3$, and H 4 , plus the C -termini of each H 2 A ) as flexible chains of beads with the first bead rigidly attached to the parent core. Each bead comprises 5 amino acids and its centred at the $\mathrm{C}_{\beta}$ atom of the middle amino acid. Each tail chain is assigned a customized intramolecular force field comprising bond stretching and bond-angle bending terms ${ }^{1,3}$. The parameters for this force field (i.e., equilibrium bond lengths and bond angles and the related force constants) are optimized to reproduce the configurational properties of the atomistic histone tails ${ }^{1,3}$. The charges of the tail beads are also optimized to reproduce the atomistic properties of the amino acids they represent. That is, each bead is assigned a charge equal to the sum of the charges on its five amino acids, multiplied by a scaling factor close to unity ( 1.12 for 0.15 M NaCl used here) that accounts for salt dependence in the effective charge.

Folded histone tails. We assign one bead per each 5 amino acids and centre it at the $\mathrm{C}_{\beta}$ atom of the middle amino acid using as reference structure the centroid of the highest populated folded cluster obtained in our REMD simulations. We limit tail flexibility by increasing the stretching, bending and torsional inter-tail-bead force constants by a factor of 100. The tails can spontaneously fold/unfold through our tailored MC move (see Supporting Material) that attempts transition between folded and flexible tails.

DNA linkers. The DNA that connects consecutive nucleosomes is treated as a chain of spherical beads that have a salt-dependent charge parameterized using the Stigter procedure ${ }^{13}$. The mechanical properties of the linker DNA chains are also considered, and described with the combined wormlike-chain (WLC) model ${ }^{14}$ of Jian et al. ${ }^{15,16}$. The equilibrium DNA inter-bead segment is 3 nm or 9 bp , thus to model NRLs of 182 bp and 209-bp we use 3 and 6 DNA beads ( 4 and 7 segments) per linker, respectively. The exiting and entering DNA linkers attached to the nucleosome define an angle of $108^{\circ}$, which corresponds to the 147 DNA base pairs tightly wound $\sim 1.7$ times around the core ${ }^{10}$.

Solvent and ionic environment. The water around the oligonucleosome is treated implicitly as a continuum. The screening of electrostatic interactions due to the presence of monovalent ions in solution ( 0.15 M NaCl ) is treated using a Debye-Hückel potential (electrostatic screening length of $1.27 \mathrm{~nm}^{-1}$ ) ${ }^{3}$ and, as described above, with the charges on each component parameterized considering salt-dependent screening.

To prevent overlap among chromatin components, each nucleosome charge, linker DNA bead, and histone tail bead are assigned an excluded volume. Specific expressions for the oligonuclesome energy and all values of parameters can be found in ${ }^{3,7,10}$.

## Monte Carlo algorithm for the simulation of chromatin

We sample our 24 -nucleosome chromatin conformations at constant temperature using a Monte Carlo (MC) procedure with five different moves.

The first three are our standard global pivot, local translation, and local rotation moves, which focus on the conformational sampling of the main oligonucleosome chain (nucleosomes joined by DNA beads). The global pivot move is implemented by randomly choosing one linker DNA bead or nucleosome core and a random axis passing through the chosen component. The shorter part of the oligonucleosome about this axis is rotated by an angle chosen from a uniform distribution within a range set so that the acceptance probability is $\sim 35 \%$. The local translation and rotation moves also select randomly an oligonucleosome chain component (linker DNA bead or core) and an axis passing through it. In the translation/rotation move, the component is then moved/rotated along/about the axis by a distance/angle sampled from a uniform distribution also chosen so that the acceptance probability is $\sim 35 \%$.

The fourth is our new tail folding/unfolding move, which implements transitions between folded and unfolded tails. This move randomly selects a histone tail chain, and either folds it and rigidifies it, or unfolds it and allows it to become flexible with probabilities P and $1-\mathrm{P}$, respectively. By changing the value of $P$, we control the concentration of folded and unfolded tails. The different chromatin conformations in the resulting equilibrium ensemble have a fixed concentration of folded/unfolded tails; however, the specific locations of the folded/unfolded tails change among the different conformations. The resulting equilibrium ensemble thus mimics an array of chromatin fibers in which the tails transiently fold and unfold.

The fifth is our tail regrowth move, which is implemented to sample flexible histone-tail conformations based on the configurational bias MC method ${ }^{17}$. This move randomly selects a histone tail chain defined as a flexible tail, and regrows it bead-by-bead using the Rosenbluth scheme ${ }^{18}$. To prevent histone tail beads from penetrating the nucleosome core, the volume enclosed within the nucleosome surface is discretized, and any trial configurations that place the beads within this volume are rejected automatically.

The first three moves are accepted or rejected based on the Metropolis criterion. The pivot, translation, rotation, tail folding/unfolding, and tail regrowth moves are attempted with probabilities of $0.2,0.1,0.1,0.2$, and 0.4 , respectively.

## Calculation of the absolute and relative packing ratios

The absolute packing ratio is a measurement of oligonucleosomes compactness, and is the defined as the number of nucleosomes per 11 nm of oligonucleosome length. To calculate this packing ratio, we compute the length of the oligonucleosome fiber axis passing. We define the fiber axis as a 3-dimensional parametric curve

$$
\begin{equation*}
\mathbf{r}^{a x}(i)=\left(r_{1}^{a x}(i), r_{2}^{a x}(i), r_{3}^{a x}(i)\right) \tag{2}
\end{equation*}
$$

where $r_{j}^{a x}(i)$ are three functions that map the center positions of the $i^{\text {th }}$ nucleosome $\mathbf{r}_{i}=\left(r_{i, 1}, r_{i, 2}, r_{i, 3}\right)$. We approximate these functions with second order polynomials of the form

$$
\begin{equation*}
r_{j}^{a x}(i) \approx P_{j}(i)=\sum_{k=1}^{3} p_{k, j} i^{(3-k)} \tag{3}
\end{equation*}
$$

by fitting the data sets $\left[r_{i}\right]$ by a least-squares procedure. We determine the coefficients of the polynomial $P_{j}(i)$ by minimizing the sum of the squares of the residuals

$$
\begin{equation*}
l_{j}=\sum_{i=1}^{N_{C}}\left(r_{i, j}-P_{j}(i)\right)^{2} \tag{4}
\end{equation*}
$$

where $N_{C}$ gives the number of nucleosome cores in an oligonucleosomes. This residual function accounts for the differences between a proposed polynomial fit and the observed
nucleosome positions. After determining the polynomial coefficients, we use Eq. (3) to produce $N_{C}$ points per spatial dimension and compute the fiber length $L_{\text {fiber }}$ as follows:

$$
\begin{equation*}
L_{\text {fiber }}=\sum_{i=1}^{\left(N_{C}-1\right) / 2}\left|\mathbf{r}^{a x}(2 i-1)-\mathbf{r}^{a x}(2 i+1)\right| \tag{5}
\end{equation*}
$$

where the distances are between every two consecutive nucleosome centres. The absolute packing ratio $P_{\mathrm{A}}$ is then calculated as the number of cores multiplied by $11 \mathrm{~nm} / L_{\text {fiber }}$. In addition, we report relative packing ratios to describe the loss of compaction upon histone tail folding more easily. We have defined these relative packing ratios as

$$
\begin{equation*}
P_{\mathrm{R}}=\left(\frac{P_{\mathrm{A}}-P_{\mathrm{O}}}{P_{\mathrm{C}}-P_{\mathrm{O}}}\right) \times 100 \% \tag{6}
\end{equation*}
$$

where $P_{\mathrm{O}}$ is the absolute packing ratio calculated for an open oligonucleosome modelled at low monovalent salt ( 0.01 M NaCl ), no LHs , and $100 \%$ flexible histone tails; and $P_{\mathrm{C}}$ is the absolute packing ratio calculated for a fully condensed oligonucleosome modelled at high monovalent salt ( 0.15 M NaCl ), no LHs , and $100 \%$ flexible histone tails. Fully compact fibers give a relative packing ratio of $100 \%$, while the low salt open fibers produce packing ratios of 0\%.

## Frequency of tail-mediated interactions.

We measure the fraction of configurations that tails of a specific kind $t(t=\mathrm{H} 4, \mathrm{H} 3, \mathrm{H} 2 \mathrm{~B}$, and H 2 A ) in a chromatin chain are 'in contact' with a specific component $c$ of the chromatin chain ( $c=a$ non-parental nucleosome or a non-parental DNA linkers) (Fig. S5b). To do this, we construct two-dimensional matrices with the following elements

$$
\begin{equation*}
T^{\prime}(t, c)=\operatorname{mean}\left[\frac{1}{N_{C} N} \sum_{i \in I_{C}} \sum_{j=1}^{N} \partial_{i, j}^{t, c}(M)\right] . \tag{7}
\end{equation*}
$$

Here $N_{C}$ is the number of nucleosomes in the chromatin array, $N$ the total number of chromatin components (nucleosomes and linker DNAs), and $I_{C}$ indicates a nucleosome particle within the chromatin chain. The mean above is taken over the converged MC configurations used for statistical analysis and

$$
\partial_{i, j}^{t, c}(M)=\left\{\begin{array}{lc}
1 & \text { if } j \text { is a c - type component 'in contact' with }  \tag{8}\\
\text { a tail of kind t of nucleosome i at MC frame } M \\
0 & \text { otherwise. }
\end{array}\right.
$$

For a MC frame $M$, we consider a specific $t$-kind tail of core $i$ to be either free or in contact with only one of the $N$ chromatin components of the oligonucleosome chain. The $t$-tail is in contact with a component of type $c$ if the shortest distance between its beads and the beads or core charges of $c$ is smaller than the shortest distance to any other type of component and also smaller than the relevant tail-component excluded volume distance (see parameters in ${ }^{10}$ ). The resulting normalized patterns of interactions provide crucial information into the frequency by which different tails mediate chromatin interactions.

SUPPORTING TABLES

| System no. | System | Protocol | Force field | Water model | Simulatio <br> n length |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | H4 tail | REMD | AMBER99SB*ILDN | TIP3P | $\begin{array}{ll} \hline 56 & \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } & \end{array}$ |
| 2 |  | REMD | AMBER99SB | TIP3P | ```56 replicas x 500 ns each``` |
| 3 |  | REMD | CHARMM36 | TIP3P | $\begin{array}{ll} 56 \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } \end{array}$ |
| 4 | H4 K16Ac tail | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's <br> KAc parameters | TIP3P | ```56 replicas x 500 ns each``` |
| 5 |  | REMD | AMBER99SB <br> Papageorgiou's <br> KAc parameters | TIP3P | 56 <br> replicas x 500 ns each |
| 6 |  | REMD | CHARMM36 + <br> Dejaegere's <br> parameters KAc | TIP3P | ```56 replicas x 500 ns each``` |
| 7 | H4 K12Ac tail | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's KAc parameters | TIP3P | ```56 replicas x 500 ns each``` |
| 8 | $\begin{array}{ll} \hline \mathrm{H} 4 & \mathrm{~K} 12,16 \mathrm{Ac} \\ \text { tail } \end{array}$ | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's <br> KAc parameters | TIP3P | $\begin{array}{ll} \hline 56 & \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } & \\ \hline \end{array}$ |
| 9 | $\begin{aligned} & \text { H4 K5,8,12Ac } \\ & \text { tail } \end{aligned}$ | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's <br> KAc parameters | TIP3P | 64 <br> replicas x 500 ns each |
| 10 | $\begin{aligned} & \mathrm{H} 4 \\ & \text { K5,8,12,16Ac } \\ & \text { tail } \end{aligned}$ | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's <br> KAc parameters | TIP3P | 64 <br> replicas x 500 ns each |
| 11 | H3 tail | REMD | AMBER99SB*ILDN | TIP3P | $\begin{array}{ll} \hline 56 \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } \end{array}$ |
| 12 | H3 tail | REMD | AMBER99SB | TIP3P | ```56 replicas x 500 ns each``` |
| 13 | H3 K14Ac tail | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's KAc parameters | TIP3P | ```56 replicas x 500 ns each``` |


| 14 | H2B tail | REMD | AMBER99SB*ILDN | TIP3P | $\begin{array}{ll} \hline 56 & \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } & \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | H2B tail | REMD | AMBER99SB | TIP3P | $\begin{array}{ll} 56 \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } \end{array}$ |
| 16 | $\mathrm{H} 2 \mathrm{~B} \quad$ K20Ac tail | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's KAc parameters | TIP3P | ```56 replicas x 500 ns each``` |
| 17 | $\begin{aligned} & \mathrm{H} 2 \mathrm{~B} \\ & \text { K5,12,15,20Ac } \\ & \text { tail } \end{aligned}$ | REMD | AMBER99SB*- <br> ILDN <br> Papageorgiou's KAc parameters | TIP3P | $\begin{array}{lll} \hline 56 & \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } & \\ \hline \end{array}$ |
| 18 | H2A tail | REMD | AMBER99SB*ILDN | TIP3P | ```56 replicas x 500 ns each``` |
| 19 | H2A tail | REMD | AMBER99SB | TIP3P | 56 <br> replicas x 500 ns each |
| 20 | H2AC tail | REMD | AMBER99SB*ILDN | TIP3P | $\begin{array}{ll} 56 & \\ \text { replicas } & \text { x } \\ 500 & \text { ns } \\ \text { each } & \\ \hline \end{array}$ |
| 21 | H2AC tail | REMD | AMBER99SB | TIP3P | ```56 replicas x 500 ns each``` |
| 22 | H4 tail | Chemical shift restraints | AMBER99SB*ILDN | TIP3P | 8 replicas x 500 ns each |
| 23 | H4 tail | Chemical shift restraints | CHARMM36 | TIP3P | 8 replicas x 500 ns each |
| 24 | H4 tail | Chemical shift restraints + MetaDynam ics | AMBER99SB*ILDN | TIP3P | 8 replicas x 500 ns each |
| 25 | H4 tail | Free MD | AMBER99SB*ILDN | TIP3P | $1 \mu \mathrm{~s}$ |
| 26 | H4 K16Ac tail | Free MD | AMBER99SB*- <br> ILDN <br> Papageorgiou's <br> KAc parameters | TIP3P | $1 \mu \mathrm{~s}$ |
| 27 | H3 tail | Free MD | AMBER99SB*ILDN | TIP3P | $1 \mu \mathrm{~s}$ |
| 28 | H2B tail | Free MD | AMBER99SB*ILDN | TIP3P | $1 \mu \mathrm{~s}$ |
| 29 | H2A tail | Free MD | AMBER99SB*ILDN | TIP3P | $1 \mu \mathrm{~s}$ |
| 30 | H2AC tail | Free MD | AMBER99SB*ILDN | TIP3P | $1 \mu \mathrm{~s}$ |
| 31 | Dinucleosome | Free MD with | AMBER99SB*- | TIP3P | $4 \mu \mathrm{~s}$ |


|  | with full wild- <br> type tails | virtual sites | ILDN <br> AMBER99+parmB <br> SC0 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 32 | Dinucleosome <br> with H4 K16Ac <br> tail, H3 K14Ac <br> tail, and wild <br> type H2B, H2A <br> and H2AC tails | Free MD with <br> virtual sites | AMBER99SB*- <br> ILDN <br> Papageorgiou's + <br> KAc parameters + | TIP3P | $4 \mu \mathrm{~s}$ |

Table S1. List of explicit solvent all-atom molecular dynamics simulations performed in this work.

| System no. | NRL | Folded tail concentration / other info | Salt Concentration | Sampling |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 182 bp | 0\% | 0.01M | 12 trajectories $x 50$ million MC steps |
| 2 | 182 bp | 0\% | 0.15M | 12 trajectories $x 50$ million MC steps |
| 3 | 182 bp | 5\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 4 | 182 bp | 10\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 5 | 182 bp | 25\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 6 | 182 bp | 50\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 7 | 182 bp | 75\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 8 | 182 bp | 90\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 9 | 182 bp | 100\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 10 | 182 bp | 5\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 11 | 182 bp | 10\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 12 | 182 bp | 25\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 13 | 182 bp | 50\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |


| 14 | 182 bp | 75\% H4 | 0.15M | 12 trajectories $x 50$ million 15MC steps |
| :---: | :---: | :---: | :---: | :---: |
| 15 | 182 bp | 90\% H4 | 0.15M | 1216 <br> trajectories $x$ 50 million MC steps |
| 16 | 182 bp | 100\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 17 | 182 bp | 5\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 18 | 182 bp | 10\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 19 | 182 bp | 25\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 20 | 182 bp | 50\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 21 | 182 bp | 75\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 22 | 182 bp | 90\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 23 | 182 bp | 100\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 24 | 182 bp | 5\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 25 | 182 bp | 10\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 26 | 182 bp | 25\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 27 | 182 bp | 50\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 28 | 182 bp | 75\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 29 | 182 bp | 90\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 30 | 182 bp | 100\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 31 | 182 bp | 5\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 32 | 182 bp | 10\% H2A | 0.15M | 12 trajectories $x 50$ million |


|  |  |  |  | MC steps |
| :---: | :---: | :---: | :---: | :---: |
| 33 | 182 bp | 25\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 34 | 182 bp | 50\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 35 | 182 bp | 75\% H2A | 0.15M | 12 trajectories x 50 million MC steps |
| 36 | 182 bp | 90\% H2A | 0.15M | 12 trajectories x 50 million MC steps |
| 37 | 182 bp | 100\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 38 | 182 bp | 0\% / charge of H4K16Ac bead reduced by 1e | 0.15M | 12 trajectories $x 50$ million MC steps |
| 39 | 182 bp | 0\% / charge of H3K14Ac bead reduced by 1e | 0.15M | 12 trajectories $x 50$ million MC steps |
| 40 | 209 bp | 0\% | 0.01M | 12 trajectories x 50 million MC steps |
| 41 | 209 bp | 0\% | 0.15M | 12 trajectories $x 50$ million MC steps |
| 42 | 209 bp | 5\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 43 | 209 bp | 10\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 44 | 209 bp | 25\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 45 | 209 bp | 50\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 46 | 209 bp | 75\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 47 | 209 bp | 90\% all tails | 0.15M | 12 trajectories $x 50$ million MC steps |
| 48 | 209 bp | 100\% all tails | 0.15M | 12 trajectories x 50 million MC steps |
| 49 | 209 bp | 5\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 50 | 209 bp | 10\% H4 | 0.15M | 12 trajectories |


|  |  |  |  | x 50 million MC steps |
| :---: | :---: | :---: | :---: | :---: |
| 51 | 209 bp | 25\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 52 | 209 bp | 50\% H4 | 0.15M | 12 trajectories x 50 million MC steps |
| 53 | 209 bp | 75\% H4 | 0.15M | 12 trajectories x 50 million MC steps |
| 54 | 209 bp | 90\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 55 | 209 bp | 100\% H4 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 56 | 209 bp | 5\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 57 | 209 bp | 10\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 58 | 209 bp | 25\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 59 | 209 bp | 50\% H3 | 0.15M | 12 trajectories x 50 million MC steps |
| 60 | 209 bp | 75\% H3 | 0.15M | 12 trajectories x 50 million MC steps |
| 61 | 209 bp | 90\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 62 | 209 bp | 100\% H3 | 0.15M | 12 trajectories $x 50$ million MC steps |
| 63 | 209 bp | 5\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 64 | 209 bp | 10\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 65 | 209 bp | 25\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 66 | 209 bp | 50\% H2B | 0.15M | 12 trajectories x 50 million MC steps |
| 67 | 209 bp | 75\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 68 | 209 bp | 90\% H2B | 0.15M | 12 trajectories $x 50$ million MC steps |
| 69 | 209 bp | 100\% H2B | 0.15M | 12 trajectories |


|  |  |  |  | x 50 million MC steps |
| :---: | :---: | :---: | :---: | :---: |
| 70 | 209 bp | 5\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 71 | 209 bp | 10\% H2A | 0.15M | 12 trajectories x 50 million MC steps |
| 72 | 209 bp | 25\% H2A | 0.15M | 12 trajectories x 50 million MC steps |
| 73 | 209 bp | 50\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 74 | 209 bp | 75\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 75 | 209 bp | 90\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 76 | 209 bp | 100\% H2A | 0.15M | 12 trajectories $x 50$ million MC steps |
| 77 | 209 bp | 0\% / charge of H4K16Ac bead reduced by 1e | 0.15M | 12 trajectories $x 50$ million MC steps |
| 78 | 209 bp | 0\% / charge of H3K14Ac bead reduced by 1e | 0.15M | 12 trajectories x 50 million MC steps |
| 79 | 191 bp | 0\% | 0.15M | 12 trajectories $x 50$ million MC steps |
| 80 | 200 bp | 0\% | 0.15M | 12 trajectories $x 50$ million MC steps |

Table S2. List of coarse-grained 24-nucleosome arrays without linker histones simulated in this work.

| Tail | Number of <br> amino <br> acids (N) | Total \% SS | Persistence <br> length ( $\left.L_{p}\right)$ | Contour <br> length <br> $\left(\begin{array}{l}\text { (N0.38 }\end{array}\right.$ <br> $\mathrm{nm})$ |
| :--- | :--- | :--- | :--- | :--- |
| H4 WT | 26 | $8.53 \pm 0.76$ | $0.44( \pm 0.02) \mathrm{nm}$ | 9.88 nm |
| H3 WT | 38 | $14.15 \pm 1.94$ | $0.79( \pm 0.02) \mathrm{nm}$ | 14.44 nm |
| H2B WT | 23 | $13.85 \pm 3.76$ | $0.69( \pm 0.02) \mathrm{nm}$ | 8.74 nm |
| H2A WT | 14 | $4.71 \pm 0.11$ | $0.76( \pm 0.02) \mathrm{nm}$ | 5.32 nm |


| H2AC WT | 9 | $7.63 \pm 0.08$ | $0.60( \pm 0.01) \mathrm{nm}$ | 3.42 nm |
| :--- | :--- | :--- | :--- | :--- |
| Titin <br> PEVK11 <br> peptide <br> (exp) | 11 | --- | $0.63( \pm 0.01) \mathrm{nm}$ | 4.18 nm |
| Titin <br> PEVK21 <br> peptide <br> (exp) | 21 | --- | $0.48( \pm 0.02) \mathrm{nm}$ | 7.98 nm |
| Polyproline <br> (exp) | $6,9,11,12,1$ <br> $3,15,20,23$, <br> $27,33,40$ | --- | $4.4( \pm 0.9) \mathrm{nm}$ | $2.28-15.20$ <br> nm |

Table S3: Persistence and contour length of histone tails.

| Protein | Total \% SS | Lp | Lp increase |
| :---: | :---: | :---: | :---: |
| H4 WT | $8.53 \pm 0.76$ | 0.44 ( $\pm 0.02) \mathrm{nm}$ | -- |
| H4 K16Ac | $12.10 \pm 0.97$ | 0.62 ( $\pm 0.02) \mathrm{nm}$ | 41\% |
| H4 K12Ac | $7.36 \pm 0.70$ | $0.60( \pm 0.01) \mathrm{nm}$ | 36\% |
| H4 diAc | $10.33 \pm 0.85$ | $0.58( \pm 0.02) \mathrm{nm}$ | 32\% |
| H4 triAc | $8.87 \pm 0.88$ | $0.57( \pm 0.01) \mathrm{nm}$ | 30\% |
| H4 tetraAc | $8.61 \pm 0.80$ | $0.57( \pm 0.02) \mathrm{nm}$ | 30\% |
| H3 WT | $14.15 \pm 1.94$ | 0.79 ( $\pm 0.02) \mathrm{nm}$ | -- |
| H3 K14Ac | $20.49 \pm 2.64$ | $0.89( \pm 0.02) \mathrm{nm}$ | 13\% |
| H2B WT | $13.85 \pm 3.76$ | $0.69( \pm 0.02) \mathrm{nm}$ | -- |
| $\begin{aligned} & \mathrm{H} 2 \mathrm{~B} \\ & \mathrm{~K} 20 \mathrm{Ac} \end{aligned}$ | $13.60 \pm 1.05$ | $0.74( \pm 0.01) \mathrm{nm}$ | 7\% |
| H2B <br> tetraAc | $18.10 \pm 2.19$ | $0.98( \pm 0.09) \mathrm{nm}$ | 42\% |

Table S4. Persistence-to-contour-length values for different lysine-acetylated histone tails.

SUPPORTING FIGURES
a WT tails REMD simulations
H4 amber99sb**-ildn:







C Acetylated-tails REMD simulations H4K16Ac amber99sb*-ildn:







H4K12,16Ac amber99sb*-ildn:


H4K5,8,12Ac amber99sb ${ }^{\star}$-ildn:



H4K5,8,12,16Ac amber99sb*-ildn:




Figure S1. Assessment of the convergence of the REMD simulations. The assessment was made by monitoring the changes in the $\alpha$-helical (columns 1 and 3 ) and $\beta$-strand (columns 2 and 4) folding propensity patterns for the lowest temperature replica over simulation time. The first 100 ns were discarded for equilibration, and the percentages of folded conformations per residue (folding propensity) computed over 100-to-150 ns (labeled 150 ns in black), 100-to-250 ns (labeled 250 ns in blue), 100-to-350 ns (labeled 350 ns in green), 100-to-450 ns (labeled 450 ns in orange), and 100-to-500 ns (labeled 500 ns in red) are shown. Plots are for the: (a) WT histone tails, (b) the H 4 tail with different force fields, and (c) the acetylated histone tails.


Figure S2. Schematic illustration of the persistence length calculation. See equation (1).


Figure S3. Correspondence between coarse-grained histone tail models and all-atom structures. (a-e) For each histone tail, the figure presents all-atom models and overlays of the locations of the histone tail beads on top of the all-atom models for: unstructured histone tails (left) and the most populated structured arrangement obtained in our REMD simulations (right). Histone tails are colour green $(\mathrm{H} 4)$, cyan $(\mathrm{H} 3)$, magenta $(\mathrm{H} 2 \mathrm{~B})$, yellow $(\mathrm{H} 2 \mathrm{~A})$, and orange (H2A C-tail). Each bead represents five consecutive amino acids and is centred on the beta carbon of the middle amino acid. Each bead of the flexible tail models has been labelled with its bead number (numbering started from the N -terminus), the sequence of amino acids represented by each bead (neutral amino acids are written in black, positively charged ones in blue, and negatively charged ones in red), and the total charge of the bead. Here, the asterisk indicates that the charge of the N - and C -termini has been considered. ( $\mathrm{f}-\mathrm{g}$ ) Attachment of the flexible and folded histone tail model into an all-atom nucleosome and its corresponding coarse grained representation. Histone cores and nucleosomal DNA are depicted in grey.
H4

H3

H2B


H4 Ac


Figure S4. Histone tails' most common folded structures. The top three panels show the structures of the three most populated clusters for the H 4 (green), H 3 (cyan), and H2B tails (magenta). The bottom panel shows the structure of the most populated cluster for the following H4 lysine acetylated versions: K16Ac (MonoAc1; green), K12Ac (MonoAc2; magenta), K12,16Ac (DiAc; purple), K5,8,12Ac (TriAc; cyan) and K5,8,12,16Ac (TetraAc; orange). The alpha helical motifs are highlighted in red and the beta motifs in blue. The residues involved in secondary structural motifs are labelled and the side chains are drawn with sticks with the polar hydrogens removed for clarity. The last residue is indicated with a black sphere and the acetylated lysines with a yellow sphere.


Figure S5. Folded H4 tails within a dinucleosome. This figure shows how the common H 4 folded structures would fit within two closely interacting nucleosomes. We have constructed this model by placing two 1 KX 5 nucleosomes on top of each other using the geometry of stacked nucleosomes in the tetranucleosome crystal structure, and replacing the H 4 tails with the most populated structures found in our REMD simulations.


Figure S6. Analysis of the effects of the force field on the results of the simulations. (a) Ensemble average and standard deviation of the percentage of residues of H4 and H4K16Ac that adopt secondary structural elements assessed from the lowest temperature replica in our REMD simulations using different force fields. For H4 and H4 K16Ac, we used three of the latest force fields for proteins: (1) AMBER99SB*-ILDN, (2) AMBER99SB, and (3) CHARMM36. Lysine acetylated parameters taken ${ }^{20}$ for AMBER99SB*-ILDN and AMBER99SB, and from ${ }^{21}$ for CHARMM36. (b) Ensemble average and standard deviation of the percentage of residues of all wild-type tails to adopt secondary structural elements assessed from the lowest temperature replica in our REMD simulations using two different force fields: (1) AMBER99SB*-ILDN, and (2) AMBER99SB. Figures (a) and (b) show that the important trend of increased secondary structure, specially $\beta$ motifs, upon acetylation remains for all force fields analysed. (c) Folding propensity per residue for H 4 and H 4 K 16 Ac and the three force fields used in (a) compared with the folding propensities calculated using experimental chemical shifts (red and blue, $\delta 2 \mathrm{D}$ method ${ }^{22}$ ). To be consistent with the experiment, for this comparison we classify the a structures as those containing either $\alpha, 3_{10}$, or $\pi$ helices, and the $\beta$ structures as those containing either isolated $\beta$ bridges or extended conformations. Note that we compare the H4K16Ac folding propensities with the experimental H4K16Q mutation instead; however, how well the K16Q mutation mimics K16Ac is controversial, because while the acetylated version opens chromatin, the mutation does not alter chromatin compaction ${ }^{23}$. (d) Secondary structure motifs obtained from MD simulations and predicted based on experimental chemical shifts. AMBER99SB*-ILDN force field $\left(\right.$ AMB $^{24}$ ): from 500 ns REMD simulations; C.S-restrained MD: from eight 500 ns replicas and
metadynamics on the end-to-end distance and number of hydrogen bonds ${ }^{25}$; C.S. $\delta 2 \mathrm{D}$ : predicted from experimentally determined chemical shifts of the H 4 tail in a nucleosome in solution using the $\delta 2 \mathrm{D}$ predictor.


Figure S7. Spatial distribution of H 4 and H 4 K16Ac tails during a 1 ss-long MD trajectory. The last amino acid of all frames were aligned together. The H4 and H4K16Ac tails are shown as grey and green ribbons, respectively.


Figure S8. Effect of the acetylation of different lysine residues in the H3 and H2B tails.
(a) Percentage of residues in various lysine-acetylated tails with secondary structure motifs.
(b) Effect of acetylation in the folding propensity for each residue separated by $\alpha$-helical and beta strand structural motifs. (c) Illustration of highest populated clusters with folded resides. a-helical motifs are coloured in red, while beta conformations in blue. The black sphere indicates the last residue of the N -tail (point of attachment to the nucleosome), while the yellow sphere denotes the acetylated lysine.
a


b


Figure S9. Modelling of histone tail folding and role of histone tails vs NRL. (a) A cartoon depicting the incorporation of the most populated folded histone tail conformation into the coarse-grained with histone tails in green (H4), cyan (H3), magenta (H2B), yellow (H2A), and orange (H2A C-tail). (b) Role of four different histone tails in mediating internucleosome interactions (i.e. the contacts between histone tails and non-parent nucleosomes or nonparent linker DNA) as a function of the nucleosome repeat length ( 147 bp of nucleosomal DNA plus the variable linker DNA length). In the 182 bp ( 35 -bp linker-DNA length ) arrays, the H 3 and H 4 tails spend more time mediating interactions with neighbouring nucleosomes, than with non-parental DNA linkers, for the 209-bp (62-bp linker-DNA length) arrays they engage more in interactions with non-parental DNA linkers.

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